

instrumental analysis skoog solution manual Textbook

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Understanding the intricacies of instrumental analysis is essential for students and professionals working in analytical chemistry. The "Skoog" solution manual serves as a vital resource, offering comprehensive solutions to the problems presented in the renowned textbook "Principles of Instrumental Analysis" by Douglas A. Skoog, Donald M. West, F. James Holler, and Stanley R. Crouch. This manual provides detailed explanations and step-by-step procedures that facilitate a deeper grasp of complex concepts in spectrophotometry, chromatography, electroanalytical methods, and other instrumental techniques. In this article, we explore the significance of the Skoog solution manual, its core components, how it enhances learning, and practical tips for effectively utilizing the resource.

Understanding the Importance of the Skoog Solution Manual

Comprehensive Learning Aid for Students and Educators

The Skoog solution manual is an indispensable companion for students aiming to master instrumental analysis. It bridges the gap between theoretical concepts and practical applications, providing detailed solutions to end-of-chapter problems. For educators, it serves as a guide to ensure accurate grading and to develop supplementary teaching materials.

Key benefits include:

- Clarification of complex problems with detailed step-by-step solutions
- Reinforcement of fundamental principles through practical examples
- Enhanced understanding of laboratory procedures and data interpretation
- Support for exam preparation and coursework assignments

Alignment with the Textbook Content

The solution manual is meticulously aligned with the content of the Skoog textbook, ensuring consistency in terminology, methodology, and conceptual explanations. This alignment helps students reinforce their learning and develop confidence in solving similar problems independently.

Core Components of the Skoog Solution Manual

Problem-Solving Strategies

The manual emphasizes effective problem-solving techniques tailored to various analytical methods. These strategies include:

- Understanding the core principles behind each technique
- Identifying relevant formulas and constants
- Applying logical reasoning to approach complex questions
- Cross-verifying calculations to ensure accuracy

Detailed Step-by-Step Solutions

Each problem is broken down into manageable steps, often accompanied by explanations that clarify the reasoning behind each action. Typical steps involve:

- Analyzing the problem statement
- Listing known and unknown parameters
- Applying relevant equations or principles
- Performing calculations with proper units and significant figures
- Interpreting the results in the context of the problem

Illustrative Diagrams and Graphs

Visual aids are integral to understanding complex data analysis. The manual includes diagrams such as calibration curves, spectra, and schematic setups of instruments to enhance comprehension.

Application of the Skoog Solution Manual in Learning and Practice

Enhancing Conceptual Understanding

By working through the solutions provided, students can gain a clearer understanding of how theoretical concepts translate into practical procedures. For example, the manual explains how to determine the limit of detection in spectrophotometry or optimize chromatography conditions.

Practicing Data Analysis and Interpretation

The manual offers problems involving real-world data sets, encouraging learners to analyze and interpret results critically. This practice improves skills in data processing, error analysis, and reporting.

Preparing for Laboratory Work

Many solutions include detailed protocols for experimental procedures, which serve as valuable references during laboratory sessions. This preparation reduces errors and increases efficiency in conducting experiments.

Tips for Effectively Using the Skoog Solution Manual

Active Problem Solving

Rather than passively reading solutions, students should attempt to solve problems independently and then consult the manual to compare approaches. This active engagement promotes better retention.

Understanding, Not Memorizing

Focus on understanding the reasoning behind each step. If a solution involves a complex calculation, ensure you comprehend why each step is necessary, which enhances problem-solving skills.

Integrating with Laboratory Practice

Use the manual alongside laboratory experiments to reinforce theoretical knowledge with practical application. Cross-referencing procedures can help in troubleshooting and refining techniques.

Developing Critical Thinking

Question the assumptions and methodologies used in solutions. Think about alternative approaches or improvements, fostering an analytical mindset.

Limitations and Considerations

Dependence on the Manual

While the solution manual is a valuable resource, over-reliance can hinder independent problem-solving abilities. It is essential to attempt problems on your own before consulting solutions.

Context-Specific Solutions

Some problems may be tailored to specific textbook editions or instructor preferences. Ensure that solutions are applicable to your course material.

Supplementary Resources

Complement the manual with other resources such as laboratory manuals, scientific journals, and online tutorials for a well-rounded understanding.

Conclusion

The "instrumental analysis Skoog solution manual" stands as a cornerstone in the educational journey of aspiring analytical chemists. Its detailed solutions, strategic problem-solving approaches, and visual aids facilitate a comprehensive understanding of instrumental techniques. By integrating this resource into study routines, students can develop confidence, improve their analytical skills, and prepare effectively for both academic assessments and professional laboratory work. Remember, the ultimate goal is to grasp the underlying principles and develop the ability to apply them creatively and accurately in various analytical scenarios. With diligent use and active engagement, the Skoog solution manual can significantly enhance your mastery of instrumental analysis.

Instrumental Analysis Skoog Solution Manual: An In-Depth Review for Educators and Students

In the realm of analytical chemistry, the Instrumental Analysis Skoog Solution Manual stands as a pivotal resource for students, educators, and professionals seeking a comprehensive understanding of laboratory techniques and problem-solving strategies. As a supplement to the widely-used textbook *Principles of Instrumental Analysis* by Douglas A. Skoog, Donald M. West, F. James Holler, and Stanley R. Crouch, the solution manual offers detailed step-by-step solutions to the exercises and problems presented within the textbook. This review aims to explore the manual's purpose, content, pedagogical value, and its role in fostering a deeper understanding of instrumental analytical techniques.

Understanding the Role of the Skoog Solution Manual in Analytical Chemistry Education

The Instrumental Analysis Skoog Solution Manual functions primarily as an auxiliary teaching tool. Its purpose is to bridge the gap between theoretical concepts and practical problem-solving skills essential for mastering instrumental analysis techniques such as spectroscopy, chromatography, electrochemical analysis, and mass spectrometry.

Key Objectives of the Manual

- Provide detailed, accurate solutions to textbook exercises
- Clarify complex concepts through step-by-step explanations
- Reinforce understanding of experimental procedures
- Facilitate self-study and exam preparation
- Support instructors in designing assessments and exercises

The manual's design emphasizes clarity and logical progression, enabling students to follow the reasoning behind each solution, thereby strengthening their analytical thinking.

Content Overview of the Instrumental Analysis Skoog Solution Manual

The manual typically covers the entire spectrum of topics addressed in the main textbook, including but not limited to:

- Fundamental principles of instrumental methods
- Spectroscopic techniques (UV-Vis, IR, atomic absorption)
- Chromatographic methods (gas chromatography, liquid chromatography)
- Electrochemical analysis
- Mass spectrometry
- Data analysis and interpretation
- Calibration and quantitative analysis

Within these broad categories, the manual offers solutions to end-of-chapter problems, practice questions, and case studies.

Sample Problem Types Addressed

- Calculations of analyte concentrations using calibration curves
- Determining detection limits and sensitivities
- Interpreting spectral data
- Designing experimental setups
- Troubleshooting common issues in instrumentation
- Data fitting and statistical analysis

The manual's comprehensive coverage ensures that students are well-equipped to handle both

theoretical questions and practical laboratory challenges.

Pedagogical Features and Methodology

The effectiveness of the Instrumental Analysis Skoog Solution Manual stems from its pedagogical approach. It emphasizes clarity, stepwise reasoning, and integration of theoretical concepts with practical calculations.

Step-by-Step Solutions

Each problem solution is broken down into logical steps:

- Restating the problem
- Listing assumptions and known data
- Applying relevant equations and principles
- Performing calculations with detailed explanations
- Interpreting results within the context of the problem

This approach helps students develop problem-solving skills and understand the rationale behind each step.

Use of Visual Aids and Diagrams

Where applicable, the manual includes:

- Diagrams of instrumentation setups
- Sample spectra or chromatograms
- Flowcharts of analytical procedures

These visual aids enhance comprehension and facilitate a more intuitive grasp of complex concepts.

Alignment with Learning Outcomes

The manual aligns solutions with learning objectives specified in the textbook, ensuring consistency and reinforcing core concepts.

Advantages and Limitations of the Solution Manual

Advantages

- Enhanced Learning: Students can verify their solutions and understand mistakes
- Time-Saving: Accelerates homework and exam preparation
- Deepened Understanding: Clarifies difficult concepts through detailed explanations
- Instructor Support: Assists in designing assignments and assessments
- Confidence Building: Encourages independent problem-solving

Limitations

- Over-Reliance Risk: Students may become dependent on solutions rather than developing problem-solving skills
- Potential for Misuse: Without proper guidance, solutions might be copied without understanding
- Updates and Editions: Variability exists across editions; some solutions may be outdated or less detailed in older versions
- Lack of Experimental Data: The manual primarily focuses on calculations and theoretical problems, offering limited guidance on actual laboratory procedures

Practical Recommendations for Use

To maximize the benefits of the Instrumental Analysis Skoog Solution Manual, users should consider the following:

- Integrate with Active Learning: Use solutions as a guide, then attempt problems independently before consulting the manual
- Supplement with Laboratory Practice: Combine problem-solving with hands-on experiments to reinforce concepts
- Discuss with Instructors: Clarify doubts and explore alternative problem-solving methods
- Focus on Understanding: Use solutions to understand the reasoning, not just to obtain answers

Comparative Analysis with Other Resources

While various solution manuals and online resources exist, the Instrumental Analysis Skoog Solution Manual distinguishes itself through:

- Its alignment with the authoritative textbook
- The depth of explanations tailored to instrumental analysis
- Its structured, pedagogical approach suitable for undergraduate and graduate students

Alternative resources, such as online tutorials, forums, or commercial review books, may lack the

cohesive structure and authoritative nature of the manual.

Conclusion: A Valuable Resource for Mastery in Instrumental Analysis

The Instrumental Analysis Skoog Solution Manual remains an invaluable resource for those engaged in learning or teaching analytical chemistry. Its detailed solutions, pedagogical clarity, and comprehensive coverage make it a reliable companion for mastering complex instrumental techniques and problem-solving skills. However, it should be used thoughtfully?as a supplement to active learning and laboratory experience?to foster genuine understanding and competence in the field.

For educators, it offers a means to facilitate effective assessment and support diverse learning styles. For students, it provides a pathway to deepen comprehension, build confidence, and excel in coursework and examinations. As analytical chemistry continues to evolve with technological advancements, tools like the Skoog solution manual will remain essential in bridging theory and practice, nurturing the next generation of analytical scientists.

In summary, the Instrumental Analysis Skoog Solution Manual exemplifies the integration of comprehensive problem-solving guidance with pedagogical finesse?an essential asset in the educational journey through instrumental analysis.

Question What topics are covered in the Skoog Instrumental Analysis Solution Manual? The Skoog Instrumental Analysis Solution Manual covers topics such as spectroscopic techniques, chromatographic methods, electroanalytical methods, sample preparation, and data analysis as presented in the textbook. **Answer** How can I effectively use the Skoog Solution Manual for understanding instrumental analysis concepts? Use the solution manual to verify your answers, understand detailed problem-solving steps, and clarify complex concepts by reviewing the provided explanations for each question. Is the Skoog Instrumental Analysis Solution Manual available for free online? Typically, the official solution manual is available through academic resources or purchase from authorized publishers. Be cautious of unauthorized free copies to ensure accuracy and respect copyright. Can the Skoog Solution Manual help in exam preparation for instrumental analysis courses? Yes, it provides worked-out solutions that can help reinforce your understanding of key concepts and improve problem-solving skills necessary for exams. Where can I find legitimate access to the Skoog Instrumental Analysis Solution Manual? Legitimate access is usually available through university libraries, official publisher websites, or by purchasing the manual through authorized vendors. Always ensure you're using authorized sources to obtain study materials.

Related keywords: instrumental analysis, skoog, solution manual, spectroscopy, chromatography, chemical analysis, lab manual, analytical techniques, qualitative analysis, quantitative analysis

INTRODUCTION TO ANALYSIS

Introduction to Analysis

Analysis is a foundational branch of mathematics that deals with understanding the behavior of functions, sequences, and structures through rigorous methods. It forms the backbone of many scientific disciplines, including physics, engineering, economics, and computer science. Whether you're exploring the limits of a function, examining the convergence of a series, or studying the properties of geometric objects, analysis provides the tools needed to delve deep into the mathematical universe. This comprehensive guide introduces the core concepts, historical development, and applications of analysis, serving as an essential resource for students and professionals alike.

What is Analysis?

Analysis, often referred to as mathematical analysis, is the study of limits, continuity, derivatives, integrals, and infinite processes. It is concerned with understanding and formalizing the concepts of change and accumulation, which are fundamental in modeling real-world phenomena.

Historical Background of Analysis

The origins of analysis trace back to the 17th century with the development of calculus by Isaac Newton and Gottfried Wilhelm Leibniz. Their groundbreaking work introduced the fundamental ideas of differentiation and integration. Over time, mathematicians formalized these concepts, leading to the rigorous foundations of analysis in the 19th century—primarily through the work of Augustin-Louis Cauchy, Karl Weierstrass, and others.

Core Objectives of Analysis

- To understand the properties of functions and sequences
- To rigorously define limits, continuity, derivatives, and integrals
- To analyze the behavior of mathematical systems under various operations
- To provide tools for solving real-world problems involving change and accumulation

Branches of Analysis

Analysis is a broad field with several interconnected branches, each focusing on different aspects of mathematical concepts.

Real Analysis

Real analysis deals with real numbers and real-valued functions. It explores the properties of sequences, series, limits, continuity, differentiation, and integration in the context of real numbers.

Complex Analysis

Complex analysis studies functions of complex variables. It involves the analysis of holomorphic functions, complex integration, and conformal mappings, with applications in physics and engineering.

Functional Analysis

This branch extends the ideas of analysis to infinite-dimensional spaces. It involves the study of function spaces, operators, and their properties, crucial in quantum mechanics and signal processing.

Fourier and Harmonic Analysis

Focuses on representing functions as sums or integrals of sinusoidal functions. It is fundamental in signal processing, acoustics, and image analysis.

Fundamental Concepts in Analysis

Understanding analysis requires familiarity with several foundational concepts that underpin the entire discipline.

Limits and Continuity

- Limit: Describes the behavior of a function as the input approaches a specific point.
- Continuity: A function is continuous if small changes in input lead to small changes in output. Formally, a function f is continuous at a point c if $\lim_{x \rightarrow c} f(x) = f(c)$.

Differentiation

Differentiation measures how a function changes at a point. The derivative $f'(x)$ indicates the slope of the tangent line to the graph of f .

Integration

Integration accumulates quantities such as area under a curve. The definite integral $\int_a^b f(x) dx$ computes the accumulation of $f(x)$ from a to b .

Sequences and Series

- Sequences: Ordered lists of numbers that approach a limit.
- Series: Sum of the terms of a sequence. Convergence or divergence of series is a central topic in analysis.

Key Theorems and Principles

Several fundamental theorems form the backbone of analysis, providing tools for understanding and solving problems.

Limit Theorems

- Squeeze Theorem: If $f(x) \leq g(x) \leq h(x)$ near a point and $\lim_{x \rightarrow c} f(x) = \lim_{x \rightarrow c} h(x) = L$, then $\lim_{x \rightarrow c} g(x) = L$.

Continuity Theorems

- Intermediate Value Theorem: If f is continuous on $[a, b]$ and d is between $f(a)$ and $f(b)$, then there exists $c \in [a, b]$ such that $f(c) = d$.

Differentiation and Integration Theorems

- Mean Value Theorem: There exists some $c \in (a, b)$ such that $f'(c) = \frac{f(b) - f(a)}{b - a}$.
- Fundamental Theorem of Calculus: Connects differentiation and integration, stating that they are inverse processes.

Applications of Analysis

Analysis has numerous applications across various fields:

- Physics: Modeling motion, electromagnetism, and quantum mechanics.
- Engineering: Signal processing, control systems, and systems analysis.

- Economics: Optimization, modeling market behavior, and risk assessment.
- Computer Science: Algorithms, numerical methods, and complexity analysis.
- Mathematics: Developing further theories in topology, differential equations, and mathematical modeling.

Learning and Studying Analysis

Mastering analysis requires a systematic approach:

- Start with the fundamentals of algebra and calculus.
- Study definitions carefully and understand the logical structure of proofs.
- Practice solving problems regularly to develop intuition.
- Explore real-world applications to see the relevance of theoretical concepts.
- Use textbooks, online courses, and educational videos for diverse perspectives.

Conclusion

Analysis is an essential and vibrant part of mathematics that underpins many scientific and engineering disciplines. Its rigorous approach to understanding the behavior of functions and sequences provides a powerful framework for solving complex problems. Whether you are a student beginning your journey or a professional applying analysis in research, a solid grasp of its principles opens up a world of intellectual exploration and practical application. Embracing the study of analysis not only enhances mathematical skills but also enriches the understanding of the natural and technological world around us.

Analysis is a foundational discipline that underpins numerous fields, from mathematics and science to economics and social sciences. Its primary purpose is to systematically examine, interpret, and understand complex data, phenomena, or concepts to uncover underlying patterns, relationships, or principles. As an intellectual pursuit, analysis enables us to transform raw information into meaningful insights, thereby informing decision-making, advancing knowledge, and fostering innovation. This comprehensive overview delves into the core aspects of analysis, exploring its origins, methodologies, types, applications, and significance in contemporary society.

Understanding the Concept of Analysis

Analysis, at its core, involves breaking down a complex whole into simpler, more manageable parts to better understand how they function individually and collectively. This process is akin to dissecting a machine to see how each component contributes to the overall operation. The fundamental goal is to identify relationships, causality, and structure within the subject under examination.

Key Characteristics of Analysis:

- Decomposition: Dividing a subject into constituent parts.
- Examination: Investigating each part thoroughly.
- Interpretation: Drawing meaningful conclusions from the parts.
- Synthesis: Reintegrating insights to understand the whole.

Analysis is both a methodology and a way of thinking?an intellectual toolkit essential for problem-solving and critical thinking.

The Origins and Evolution of Analysis

The roots of analysis trace back to ancient civilizations, where early mathematicians and philosophers sought methods to quantify and understand the world. However, it was during the 17th and 18th centuries that analysis emerged as a formal discipline.

Historical Milestones:

- Ancient Greece: Philosophers like Aristotle laid early groundwork by categorizing and dissecting ideas and natural phenomena.
- Mathematics: The development of calculus by Isaac Newton and Gottfried Wilhelm Leibniz in the 17th century marked a pivotal moment, providing tools to handle change and motion mathematically.
- 19th Century: Formalization of analysis as a branch of mathematics, focusing on limits, continuity, and rigorous proofs, primarily through the work of Augustin-Louis Cauchy and Karl Weierstrass.
- Modern Era: Expansion into various fields such as data analysis, qualitative analysis in social sciences, and computational analysis with the advent of computers.

Over time, analysis has evolved from a purely mathematical activity to a versatile approach applicable across disciplines, emphasizing systematic inquiry and empirical evaluation.

Different Types of Analysis

Analysis manifests in various forms depending on the context, purpose, and nature of the subject matter. Here, we explore some of the most prominent types.

Mathematical Analysis

Mathematical analysis deals with functions, limits, derivatives, integrals, and infinite series. It provides the rigorous foundation for calculus, enabling precise examination of change, accumulation, and structure in mathematical models.

Key aspects include:

- Real Analysis: Focuses on real numbers and real-valued functions, exploring concepts like continuity, convergence, and measure theory.
- Complex Analysis: Extends analysis into the complex plane, studying functions of complex variables, with applications in engineering and physics.
- Functional Analysis: Investigates spaces of functions and their transformations, crucial for quantum mechanics and differential equations.

Data Analysis

In the contemporary digital age, data analysis involves examining large datasets to extract meaningful patterns and insights. It combines statistical techniques, computational algorithms, and visualization tools.

Main components:

- Descriptive Analysis: Summarizes data characteristics through measures like mean, median, and standard deviation.
- Inferential Analysis: Draws conclusions and makes predictions about populations based on samples.
- Predictive Analysis: Uses historical data to forecast future trends.
- Prescriptive Analysis: Recommends actions based on data insights.

Qualitative Analysis

Used predominantly in social sciences, qualitative analysis interprets non-numerical data such as interviews, observations, and texts to understand meanings, experiences, and social phenomena.

Methods include:

- Content analysis
- Thematic coding
- Discourse analysis

Scientific Analysis

In scientific research, analysis involves designing experiments, collecting data, and interpreting results to validate hypotheses or establish new theories.

Types include:

- Experimental analysis
- Statistical analysis
- Comparative analysis

The Methodology of Analysis

Effective analysis follows a structured approach, often iterative, to ensure thorough understanding and reliable conclusions.

Typical steps include:

- Defining the Objective: Clarify what questions need answering.
- Data Collection: Gather relevant data through experiments, surveys, observations, or literature.
- Data Processing: Clean, organize, and prepare data for examination.
- Decomposition: Break down the subject into parts or features.
- Examination: Analyze each component using appropriate techniques.
- Interpretation: Derive insights, identify patterns, and establish relationships.
- Synthesis: Integrate findings into a comprehensive understanding.
- Validation: Verify results through replication, peer review, or cross-validation.
- Reporting: Communicate findings clearly and accurately.

This methodology emphasizes rigor, transparency, and critical evaluation at every stage.

Applications of Analysis Across Disciplines

Analysis is integral to numerous fields, each with unique methodologies and objectives.

In Mathematics and Engineering

Analysis underpins the development of models for physical systems, optimization problems, and algorithms. For example:

- Analyzing the stability of structures.
- Optimizing network flows.
- Designing control systems.

In Economics and Finance

Economic analysis helps understand market behaviors, policy impacts, and financial risks.

- Welfare analysis
- Cost-benefit evaluations
- Portfolio analysis

In Social Sciences and Humanities

Qualitative and quantitative analyses uncover social trends, cultural patterns, and human behaviors.

- Sociological surveys
- Historical document analysis
- Literary critique

In Data Science and Technology

Data analysis fuels artificial intelligence, machine learning, and big data applications.

- Pattern recognition
- Natural language processing
- Predictive modeling

Significance and Challenges of Analysis

The value of analysis lies in its capacity to transform complexity into clarity. It enables informed decision-making, innovation, and scientific advancement.

Key benefits include:

- Enhanced understanding: Clarifies intricate phenomena.
- Problem solving: Identifies root causes and solutions.

- Forecasting: Anticipates future developments.
- Innovation: Inspires new ideas and approaches.

However, analysis also faces challenges:

- Data quality: Inaccurate or incomplete data can lead to misleading conclusions.
- Bias: Subjectivity can distort interpretation.
- Complexity: Highly intricate systems may resist straightforward analysis.
- Overfitting: Excessive focus on data nuances may impair generalizability.

Addressing these challenges requires methodological rigor, transparency, and ongoing validation.

The Future of Analysis

As technology advances, analysis continues to evolve, becoming more sophisticated and accessible. Notable trends include:

- Big Data Analytics: Managing and interpreting vast datasets.
- Machine Learning and AI: Automating complex analysis and pattern recognition.
- Interdisciplinary Approaches: Integrating methods across fields for holistic insights.
- Real-Time Analysis: Enabling immediate decision-making in dynamic environments.

Furthermore, ethical considerations surrounding data privacy and responsible interpretation are increasingly prominent, emphasizing the importance of integrity in analytical practices.

Conclusion

Analysis stands as a cornerstone of human intellectual activity, empowering us to navigate an increasingly complex world. From its mathematical foundations to its applications in technology, science, economics, and beyond, analysis equips us with tools to decipher patterns, understand systems, and make informed decisions. Its evolution reflects humanity's relentless pursuit of knowledge and mastery over the unknown. As new challenges and opportunities emerge, the discipline of analysis will undoubtedly continue to adapt and expand, remaining vital in shaping our understanding of the universe and our place within it.

Question What is the main goal of analysis in mathematics? The main goal of analysis is to rigorously study limits, continuity, derivatives, integrals, and infinite series to understand the behavior of functions and sequences. How does calculus relate to analysis? Calculus is a fundamental part of analysis, focusing on derivatives and integrals, and provides the tools and

concepts used to analyze change and accumulation in mathematical functions. What are the key foundational topics in an introduction to analysis? Key topics include limits, continuity, sequences and series, differentiation, integration, and the topology of real numbers. Why is the rigorous approach important in analysis? A rigorous approach ensures that mathematical concepts are well-defined and proofs are logically sound, which is essential for establishing solid mathematical foundations. What is the significance of the epsilon-delta definition in analysis? The epsilon-delta definition provides a precise way to define limits and continuity, making concepts that seem intuitive into formal mathematical statements. How does real analysis differ from basic calculus? Real analysis delves into the theoretical and foundational aspects of calculus, providing rigorous proofs and exploring the underlying structures, whereas basic calculus focuses on computational techniques and applications.

Related keywords: mathematical analysis, real analysis, calculus, limits, continuity, derivatives, integrals, sequences and series, epsilon-delta definition, functions

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